Radiative Transfer in Protoplanetary Disks

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Outline

- Context: Circumstellar Disks around Young Stars
- Elements of continuum radiative transfer
- Constraints from various techniques:
 - thermal emission & spectroscopy,
 - light scattering,
 - polarization,
 - infrared interferometry
- Multi-technique modelling
- Observation & modelling of Gas in disks



From clouds to envelopes, to disks, to planets







From clouds to envelopes, to disks, to planets

Timescale for gas dispersal and planet formation?
Grain growth and settling ?
Relative evolution of dust and gas ?

Processes in Protoplanetary disks



Dust in Protoplanetary disks

• Dust grains are expected to grow by coagulation and to settle by gravity

• Disks should have a stratified structure

• Physical models predict extremely short timescales (<10⁵ yrs) for both phenomena

• Disks around 10⁶ yr-old T Tauri stars could already show evidence for these effects

The search for stratified disks is on !

A variety of observations

Each approach probes a different part of the disk

Disk modelling must consider as many observations as possible at once

Multi-λ modelling Not so frequent ... but necessary!



⇒ Radiative transfer code (MCFOST)

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How to extract information from observations?

1) Goal: obtain simple, parametric fit to as wide a set of observations as possible

- A few simplistic asumptions:

 parametric description of disk structure
 Mie theory
- exact radiative transfer: MCFOST
- systematic exploration of the parameter space
- **x**2 fitting, Bayesian estimates
- ⇒ Quantify parameters AND their validity range
- 2) Link with models of the physics of disks

Radiative transfer in dust

$$\frac{dI_{\lambda}(\overrightarrow{r},\overrightarrow{n})}{ds} = -\kappa_{\lambda}^{\text{ext}}(\overrightarrow{r}) I_{\lambda}(\overrightarrow{r},\overrightarrow{n})
+ \kappa_{\lambda}^{\text{abs}}(\overrightarrow{r}) B_{\lambda}(T(\overrightarrow{r}))
+ \kappa_{\lambda}^{\text{scatt}}(\overrightarrow{r}) \frac{1}{4\pi} \int_{\Omega} \psi_{\lambda}(\overrightarrow{r},\overrightarrow{n}',\overrightarrow{n}) I_{\lambda}(\overrightarrow{r},\overrightarrow{n}') d\Omega'$$

and

$$4\pi M(\overrightarrow{r}) \int_0^\infty \kappa^{\mathrm{abs}}(\lambda, \overrightarrow{r}) B_\lambda(T(\overrightarrow{r})) \, d\lambda = \Gamma^{\mathrm{abs}}(\overrightarrow{r})$$

Radiative transfer in dust



$$4\pi M(\overrightarrow{r}) \int_0^\infty \kappa^{\mathrm{abs}}(\lambda,\overrightarrow{r}) B_\lambda(T(\overrightarrow{r})) \, d\lambda = \Gamma^{\mathrm{abs}}(\overrightarrow{r})$$

Why the need for Monte Carlo?

- multiple-scattering
- anisotropic scattering (+ polarisation)
- complex 3D structure
- benchmark: tested up to very high optical depths (10⁶)
 Fast: variance reduction techniques, MC + diffusion approx., MC + ray-tracing

Lefevre et al 1982, 1983

Bjorkman & Wood, 2001 Wolf, 2003 Niccolini, 2003 Juvela, 2005 Pinte et al, 2006, 2009



MCFOST

MCFOST? - 3D radiative transfer Monte Carlo method - radiative transfer in dust and gas

Physical processes:

- multiple scattering
- and polarisation
- dust heating
- NLTE molecular pop.

Code specificities:

- Spatial differentiation (radial/vertical)
- No limits on opacity: $\tau_V = 0 \rightarrow 10^9$
- Non-equilibrium grains: PAHs, VSGs
- consistent modeling of dust and gas phases
- ⇒ scattered light (+ pola) & thermal emission maps + SEDs
- + visibilities + molecular emission maps & line profiles

Disk Emission

- The disk is reprocessing the stellar light
- hot surface + warm/cool midplane
- T ranges from 1500K (Rin) to 30K (Rout, midplane)
- ⇒ disk radiates from NIR to mm/cm regime





IR spectroscopy with Spitzer



Grains grow to µm sizes in the surface

v. Boekel et al 2003

Thermal emission at mm wavelengths

Emission from a pole-on disk:

 $F_{\nu} =$

$$\frac{1}{D^2} \int_{R_{in}}^{R_{out}} B_{\nu}(T(r))(1 - e^{-\tau(\nu, r)}) 2\pi r dr$$

Dust opacity strongly dependent on grain size $\tau(\nu) \propto \kappa(\nu) \propto \nu^{\beta}$

Optically thin regime: $F_{\nu} \propto \nu^2 \tau(\nu) \propto \nu^2 \kappa(\nu) \propto \nu^{(2+\beta)}$

D'Alessio et al 2001



Dust opacity indices

Measure of β

Korner et al 1995 Calvet et al 2002 Testi et al 2003 Natta et al 2004 Wilner et al 2005 Rodmann et al 2006 Lommen et al 2009



Opacity indices < 2 ⇒ Grains grow to centimeter size boulders

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Rodman et al 2006

First evidence of differential grain growth ?

β might be larger in central parts of the disk → ALMA

See also Guilloteau et al 2010



Isella et al 2010

Multi- λ scattered light images

Dust opacity decreases with increasing λ
 Images in the thermal IR probe deeper into the disks than optical/NIR images

• Scattering depends on grain size and , and is most sensitive to $2\pi a \approx \lambda$ grains

Optical/NIR ⇔ 0.1-0.5 µm dust grains
Thermal IR ⇔ 1-5 µm dust grains

A powerful tool to probe stratification

Light scattering: anisotropy

Polarisability depends on grain size

Mie theory



grain size distribution dn(a) α a^{-3.5} da

The case of GG Tau

A 0.13M, 180AU-radius circumbinary ring
Clear detection of the ring in scattered light
Morphology extremely similar to visible image

ISM dust models match the visible Image with i $\approx 40^{\circ}$





1"

A first direct evidence

Scattered light at L' comes from 25AU above the midplane; I band, 50AU above
Arguably the most direct evidence of dust stratification to date *Settling and/or growth?*





The GG Tau ring

0.5 - 3.8 µm scattered light images

- Large grains (>1µm) are present in the disk
- The larger the deeper

⇒ Disk stratification



Duchêne et al 2004

GG Tau: models with dust stratification



Pinte et al. (2007)

GG Tau: a stratified ring

Model with stratification reproduces images from 0.5 to 3.8µm



SPH simulations (Fouchet, Gonzalez, Lyon) + **radiative transfer** Pinte et al 2007

Dust grains properties



HD 181327 (debris disk).

The dust is more evolved (2nd generation)

Inclinaison: 32°

Evidence of non spherical grains



Signatures of agregates ?



Polarisation

Polarisation by scattering very sensitive to dust properties <u>Mueller matrix (Mie theory)</u>



Circular polarisation in case of multiple scattering

$$\begin{pmatrix} I = 1 \\ Q = 0 \\ U = 0 \\ V = 0 \end{pmatrix} \overset{1^{\text{`ere}} \text{diff}}{\longrightarrow} \begin{pmatrix} I = 1 \\ Q \neq 0 \\ U = 0 \\ V = 0 \end{pmatrix} \overset{2^{\text{`eme}} \text{diff}}{\longrightarrow} \begin{pmatrix} I = 1 \\ Q \neq 0 \\ U \neq 0 \\ V \neq 0 \end{pmatrix}$$

Polarisability of dust grains Polarisability depends on grain size



Mie theory

grain size distribution $dn(a) \propto a^{-3.5} da$

Polarisability of dust grains

Polarisability depends on grain size & composition/porosity (real part of refractive index)



Mie theory

grain size distribution $dn(a) \propto a^{-3.5} da$

Effect of chemical composition/porosity

Scattering phase function & polarisability both depend on grain composition & porosity

Porous grains produce larger polarization for same asymmetry parameter

need to constrain g → multi-technique analysis



The GG Tau ring



 Intensity map: effect of anisotropic scattering clearly visible g ≈ 0.6
 ⇒ grains with size ≈ λ

The GG Tau ring



Intensity map:
 effect of anisotropic
 scattering clearly visible
 g ≈ 0.6
 ⇒ grains with size ≈ λ

 ● Polarization map: high polarisation
 ⇒ "Rayleigh" scattering
 Not reproduced by compact silicates
The GG Tau ring



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Suggests grains with low refractive index: porous grains or ices

Solution is not unique !!!

Models with well-mixed dust population can also reproduce but this requires an "exotic" dust size distribution

dn(a) α a^{-5.5} da





... polarization can help !!!

Using polarimetry to refine the model



Observations

Model with strat

without strat

Another example: AU Mic



SED and images can be reproduced both with compact and porous dust grains

Large polarisation → porous grains (ices)

Fitzgerald et al 2007



20

30

projected distance (AU)

80

100

60

50

14

10

Another example: AU Mic



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Unresolved polarimetry: tomography of inner disk

Tool to probe the disk-star interface

The magnetospheric accretion predicts formation of warp at the inner edge



Figure from Romanova et al 2004

Unresolved polarimetry: tomography of inner disk

Tool to probe the disk-star interface

The magnetospheric accretion predicts formation of warp at the inner edge

 \Rightarrow can eclipse the star

≈ 0.025 AU

Figure from Romanova et al 2004

Tomography of the inner disk

Wood et al 1996 Ménard et al 2003 O'Sullivan et al 2005

AA Tau synoptic monitoring Many rotation periods



Quick summary: Need variable achromatic extinction → occultation by a "deformed" disk

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Photo-polarimetric variation



Variations along Q axis \Rightarrow disk oriented east-west & disk inclination $\approx 70^{\circ}$



Ménard et al 2003

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Ménard et al 2003

Variations along Ω axis \Rightarrow disk orie







Measuring the inner radius of disks

Characteristic NIR size measured by interferometers < 1 AU: comparable to the location of terrestrial planets in more evolved systems

Ring model:

simple emission model: unresolved central star + narrow ring

relative contribution from star & disk estimated from SED



Radii inferred from interferometry larger than predicted



Millan-Gabet et al 2006

Radii inferred from interferometry larger than predicted



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accretional heating? lower sublimation temperature? smaller dust grains? photoevaporation? magnetospheric truncation? scattered light?

Millan-Gabet et al 2006

Measuring the inner radius of disks

Ring model justification

NIR emission only comes from the hottest dust disk are optically thick : shielding by the inner disk → further drop in dust temperature scattered light from inner disk is negligible

Introduced at the beginning to study Herbig Ae/Be stars (Tuthill et al. 2001)

Improved sensibility: T Tauri stars can now be studied (Akeson et al 2005 ; Eisner et al 2007)

⇒ Is the assumption on scattered light still valid for T Tauri stars ?

Why should we care about scattered light?

Peak of the photosphere moving towards longer λ Fraction of stellar (and then also scattered) light is larger

Albedo can be large in the NIR ! between 0.4 and 0.9 at 2.2 µm, depending on grain sizes and dust composition



Inner radius of T Tauri stars Inner radius measured by IR interferometry apparently larger than sublimation radius for T Tauri stars

But models were **neglecting** scattered light, which is the dominant contribution

→ over-estimation by factor 2

Need for detailed RT codes like MCFOST

Interpretation of AMBER data: Tatulli et al 2008 Benisty et al 2010 Olofsson et al 2010 Tatulli et al 2010



Pinte et al 2008

What radius would have been measured ?





Scattered light is a sufficient explanation

The location of fitted inner radii mimics very well the distribution of data points

Multi- λ modelling of IM Lupi

A single model with **mild stratification** remarkably reproduces all observations: $H(1mm) \approx 0.5 H(1\mu m)$



M_{dust}, grain growth & settling

Pinte et al 2008

WFPC2 0.6 µm



IM Lupi: quantitative constraints **Bayesian method** to estimate model parameters: for SED

≈ 400 000 models
Some parameters
fixed from data
(a_{max}, M_{dust}, R_{out})
→ Fitting for 6
parameters

Pinte et al 2008



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Gas & Dust evolution

• Gas represents 99% of the disk mass

• Difficult to observe but Herschel is opening the far-IR window

• Gas & dust evolution strongly coupled



Fedele et al. 2009

Gas in Protoplanetary Systems

Statistical survey (≈ 250 disks) : evolution of gas and dust from young gas-rich protoplanetary disks, to old "dry" debris disks:

• Ages 1 - 30 Myr, M to A stars, disk dust mass ($10^{-2} - 10^{-5}$ Mo)

•Well-known star-forming regions (Taurus, TW Hydra, η Cha, β Pic, Tuc Hor, Upper Sco, Herbig Ae/Be)

• Key far-IR tracers: [OI], [CII], H₂O, CO + Phot. at 70 & 160µm



Modelling tools: MCFOST + ProDiMo

Interpretation of line observations is complex !→ need for detailed modelling.

MCFOST: 3D continuum & line radiative transfer (Pinte et al 2006, 2009)

+ **ProDiMo**: thermal balance & chemistry (Woitke et 2009, Kamp et al 2010)

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Modelling tools: the DENT grid

Grid of \approx 300 000 disk models:

• sample the disk parameters observed by GASPS

• thermo-chemical structure: T_{dust}, T_{gas}, abundances

• SEDs

• 29 line fluxes and profiles: [OI], [CII], ¹²CO, o-H₂O, p-H₂O

→ Statistical tool

Woitke et al 2010 Kamp et al, in prep. Ménard et al, in prep.

stellar parameter			
M_{\star}	stellar mass $[M_{\odot}]$		0.5, 1.0, 1.5, 2.0, 2.5
age	age [Myr]		1, 3, 10, 100
$f_{ m UV}$	excess UV $f_{\rm UV} = L_{UV}$	L_{\star}	0.001, 0.1
disc parameter			
M _d	disc dust mass $[M_{\odot}]$		$10^{-7}, 10^{-6}, 10^{-5}, 10^{-4}, 10^{-3}$
$\delta = \rho_{\rm d}/\rho_{\rm g}$	dust/gas mass ratio		0.001, 0.01, 0.1, 1, 10
$R_{\rm in}$	inner disc radius [R_{sub}]	di]	1, 10, 100
Rout	outer disc radius [AU]]	100, 300, 500
ϵ	column density $N_{\rm H}(r)$	$\propto r^{-\epsilon}$	0.5, 1.0, 1.5
β	flaring $H(r) = H_0 \left(\frac{r}{r_0}\right)^{t}$	β	0.8, 1.0, 1.2
dust parameter			
S	settling $H(r, a) \propto H(r)$) $a^{-s/2}$	0,0.5
a_{\min}	minimum grain size [/	μ <i>m</i>]	0.05, 1
radiative transfer parameter			
i	inclination 0)°, 41.41°,	60°, 75.52°, 90° (edge-on)

200 000 cpu-hours (ANR "Dusty Disk" supercomputer, PI: F. Ménard)

Main heating mechanisms

Pinte et al 2010

● Herbig Ae/Be stars: line flux correlates with L★

• T Tauri stars: UV excess required to interpret line flux


Main heating mechanisms

Pinte et al 2010

Herbig Ae/Be stars: line flux correlates with L★

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• suggestion that L_{acc} could play a role

 \bullet No apparent correlation with L_X



HD 169142

Dust modelling (SED + images) to constrain the disk structure and dust properties

- → geometry, gap at 10 AU
- \rightarrow amount of PAHs: $f_{PAH}=0.03$

Input for gas modelling
→ low UV excess
→ PAH = main gas heating source

→ gas dust ratio \approx 20-50

Meeus et al 2010

Similar work for the T Tauri star TW Hydra, see Thi et al 2010



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observed model

Table 1. Summary of the PACS targeted lines and the CO lines that were observed with the SMA (Raman et al. 2006, Panić et al. 2008). We list the central wavelength, continuum and line flux or upper limits (three sigma) in the case of a non-detection. Between brackets we give the one sigma statistical error for the detections.

Species	Transition	λ_c (μ m)	Continuum (Jy)	Line Flux (10 ⁻¹⁸ W/m ²)
[OI]	${}^{3}P_1 \rightarrow {}^{3}P_2$	63.18	18.89 (0.13)	71.7 (3.8)
[OI]	${}^{3}P_{0} \rightarrow {}^{3}P_{1}$	145.53	13.76 (0.03)	< 10.4
[CII]	$^2P_{3/2} \rightarrow ~^2P_{1/2}$	157.74	14.48 (0.03)	< 6.4
- II O	0 1	170 52	12 12 (0.05)	. 0 0

HD169142 in PAHs

Imaging in Mid-IR
VISIR observations
→ disk resolved in continuum and PAHs bands

Model consistent with observations → confirms amount of PAHs and geometry of the disk surface

See also Lagage et al, 2006 and Doucet et al, 2007





Spatial origin of the lines

HD 169142



Effect of X-ray irradiation



G.Aresu et al, 2010 Far-IR lines significantly affected only if $L_X \ge 10^{31}$ erg/s

Effect of X-ray irradiation



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Concluding remarks

A variety of datasets = finer disk models

 Spatial differentiation is frequent in disks around T Tauri stars

• Similar studies in Herbig Ae disks, disks around brown dwarfs and debris disks are now possible

• Testing the physics of dust grains towards planet formation: separate dust populations, non-spherical aggregates?

• Combining fine-structure lines, CO sub-mm lines and dust observations + detailed modelling is a powerful diagnosis: main gas heating mechanism, dust-to-gas ratios, ...